

No quiz today, 3.2 HW is due  
today.

Questions on 3.3 HW??

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$as\ x \rightarrow -\infty, \quad y \rightarrow \underline{\quad}$ $as\ x \rightarrow \infty, \quad y \rightarrow \underline{\quad}$	
<p>10. Equation: <math>h(x) = 2(x - 3) + 1</math></p> <p>What I know about this function: <math>2x - 6 + 1</math> <math>2x - 5</math></p> <p>linear</p> <p><math>m</math> is <math>+2</math></p> <p>End behavior:</p> <div style="border: 1px solid red; padding: 5px; display: inline-block;"> <math>as\ x \rightarrow -\infty, \quad h(x) \rightarrow \underline{-\infty}</math>  <math>as\ x \rightarrow \infty, \quad h(x) \rightarrow \underline{\infty}</math> </div>	<p>Graph:</p>

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**Linear:**

- Standard form:  $ax + by = c$   
 $\frac{by}{b} = \frac{-ax + c}{b}$   
 $y = -\frac{a}{b}x + \frac{c}{b}$   
 $-\frac{a}{b}$ : slope  
 $\frac{c}{b}$ : y-intercept
- Slope-intercept form:  $y = mx + b$   
 $m$ : slope  
 $b$ : y-intercept
- Point-slope form:  $y = m(x - x_1) + y_1$   
 $m$ : slope  
 $(x_1, y_1)$ : point on graph

**Quadratic:**

- Standard form:  $y = ax^2 + bx + c$   
 $c$ : y-intercept
- Factored form:  $y = a(x - r_1)(x - r_2)$   
 $r_1, r_2$ : x-intercepts, roots, solutions, zeroes
- Vertex form:  $y = a(x - h)^2 + k$   
 vertex:  $(h, k)$

For each, write what you know about the function (including end behavior) and then graph.

7. Equation: $f(x) = (x - 3)(x + 4)$	Graph: <div style="border: 1px solid black; width: 100%; height: 100%; position: relative;"> </div>
What I know about this function:	
End behavior:	

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**Linear:**

1. Standard form:  $ax + by = c$   
 $\frac{by}{b} = \frac{-ax + c}{b}$   
 $y = -\frac{a}{b}x + \frac{c}{b}$   
 $-\frac{a}{b}$ : slope  
 $\frac{c}{b}$ : y-intercept

2. Slope-intercept form:  $y = mx + b$   
 $m$ : slope  
 $b$ : y-intercept

3. Point-slope form:  $y = m(x - x_1) + y_1$   
 $m$ : slope  
 $(x_1, y_1)$ : point on graph

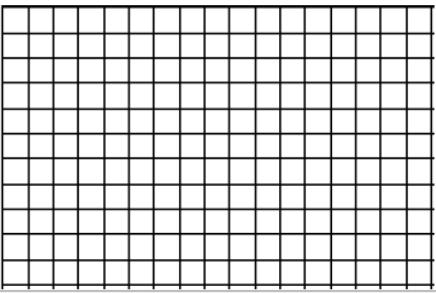
**Quadratic:**

4. Standard form:  $y = ax^2 + bx + c$   
 $C$ : y-intercept

5. Factored form:  $y = a(x - r_1)(x - r_2)$   
 $r_1$  &  $r_2$ : x-intercepts, roots, solutions, zeroes

6. Vertex form:  $y = a(x - h)^2 + k$   
vertex:  $(h, k)$

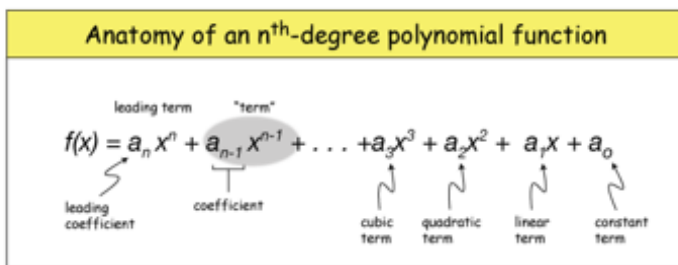
For each, write what you know about the function (including end behavior) and then graph.

<p>7. Equation: <math>f(x) = (x - 3)(x + 4)</math></p>	<p>Graph:</p> 
<p>What I know about this function:</p>	
<p>End behavior:</p>	

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# Factoring Review

*Notation for polynomials:*



A **trinomial** has three terms.

A **binomial** has two terms

**Greatest common factor:**

The first thing you should do when factoring a polynomial is to look for the largest factor common to every term. The greatest common factor of a polynomial is the greatest common factor of the coefficients times the greatest common factor of the variable(s) in the terms.

EXAMPLE: Factor  $8p^6q^2 - 4p^5q^3 + 10p^4q^4$ .

$$\begin{array}{c}
 \textcircled{2} \cdot \textcircled{2} \cdot \textcircled{2} \cdot \textcircled{p \cdot p \cdot p \cdot p \cdot p \cdot p} \cdot \textcircled{q \cdot q} - \textcircled{2} \cdot \textcircled{2} \cdot \textcircled{p \cdot p \cdot p \cdot p \cdot p} \cdot \textcircled{q \cdot q \cdot q} + \textcircled{2} \cdot \textcircled{5} \cdot \textcircled{p \cdot p \cdot p \cdot p} \cdot \textcircled{q \cdot q \cdot q \cdot q} \\
 2p^4q^2(4p^2 - 2pq + 5q^2)
 \end{array}$$

The greatest common factor of the coefficients 8, -4, and 10 is 2.

The greatest common factor of  $p^6$ ,  $p^5$ , and  $p^4$  is  $p^4$ .

The greatest common factor of  $q^2$ ,  $q^3$ , and  $q^4$  is  $q^2$ .

So we can factor out  $2p^4q^2$ , and

$$8p^6q^2 - 4p^5q^3 + 10p^4q^4 = 2p^4q^2 \cdot 4p^2 - 2p^4q^2 \cdot 2pq + 2p^4q^2 \cdot 5q^2 = 2p^4q^2(4p^2 - 2pq + 5q^2)$$

**Check** your factorization by distributing. You should end up with your original polynomial.

If the terms of a polynomial have no common factors, the polynomial is **prime**.

When the leading coefficient is a negative number, we generally factor out a common factor with a negative coefficient. Thus:  $-2x^3 + 6x^2 - 2x = -2x(x^2 - 3x + 1)$

YOUR TURN: Factor out the greatest common factor.

a)  $6a^2x^3 + 20a^3x^5 - 4a^5x^3$

$$\underline{2a^2x^3}(3 + 10ax^2 - 2a^3)$$

$$\frac{6a^2x^3}{2a^2x^3} = 3 \quad \frac{20a^3x^5}{2a^2x^3} = 10ax^2$$

b)  $-4x - 24$

$$-4(x + 6)$$

c)  $-3a^4 - 6a^2 + 3a$

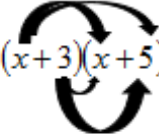
$$-3a(a^3 + 2a - 1)$$

d)  $16t^8 + 40t^5 - 24t$

$$8t(2t^7 + 5t^4 - 3)$$

**Factoring trinomials of the type  $x^2 + bx + c$ :**

Recall the FOIL method of multiplying two binomials:

$$(x+3)(x+5) = x \cdot x + x \cdot 5 + 3 \cdot x + 3 \cdot 5 = x^2 + 3x + 5x + 15 = x^2 + 8x + 15$$


To factor a trinomial in the form  $x^2 + bx + c$ , we undo the FOILing process. If a trinomial in this form can be factored, the factorization will look like this:  $(x+p)(x+q)$ , where  $p$  and  $q$  are two numbers whose product is  $c$  and whose sum is  $b$ .

EXAMPLE: Factor  $x^2 + 9x + 8$ .

$x^2 + 9x + 8 = (x + \underline{\quad})(x + \underline{\quad})$ . To fill in the blanks, find two numbers whose product is 8 and whose sum is 9.

Factors of 8: 2, 4 and 8, 1

$2 + 4 = 6$ ,  $8 + 1 = 9$ . The two numbers we are looking for are 8 and 1

So  $x^2 + 9x + 8 = (x + 8)(x + 1)$

Use these patterns when factoring a trinomial in the form  $x^2 + bx + c$ :

If  $c$  is **negative**, one of its factors will be negative, one will be positive.

If  $c$  is **positive** and  $b$  is **negative**, both factors of  $c$  will be negative.

If  $c$  is **positive** and  $b$  is **positive**, both factors of  $c$  will be positive.

If a trinomial cannot be factored, it is **prime**.

**Check** your factorization by **FOILing** it out. You should get the original trinomial.

YOUR TURN: Factor each of the following trinomials.

a)  $y^2 + 5y + 6$

$$(y+2)(y+3)$$

b)  $x^2 - 7x + 12$

$$(x-4)(x-3)$$

c)  $y^2 + 5y - 36$

$$(y+9)(y-4)$$

d)  $x^2 - 7x - 30$

$$(x-10)(x+3)$$

e)  $x^3 - x^2 - 30x$  (HINT: Factor out the greatest common factor first.)

$$x(x^2 - x - 30) = x(x-6)(x+5)$$



Factoring trinomials of the type  $ax^2 + bx + c$ :

Let's work through this using the trinomial  $3x^2 - 10x - 8$ . If this factors, it will factor to two binomials  $(\underline{\quad} + \underline{\quad})(\underline{\quad} + \underline{\quad})$

- List possible First terms whose product is  $ax^2$ . Write them as the first terms in each binomial factor.

$3x^2 = 3x \cdot x$  so the factorization starts looking like this:  $(3x + \underline{\quad})(x + \underline{\quad})$

- List possible Last terms whose product is  $c$ .

Factors of  $-8$  :  $1, -8$        $-8, 1$        $2, -4$        $-4, 2$   
                                   $-1, 8$        $1, -8$        $-2, 4$        $4, -2$

- Use the correct set of factors, in the correct order, so that the sum of the products of the Outside terms and the Inside terms is equal to  $bx$ .

Try:  $(3x+1)(x-8)$ . Since  $(3x)(-8) + (1)(x) = -23x \neq -10x$ , this doesn't work

HINT: Changing the signs on 1 and -8 will give  $23x$ , which also won't work.

$(3x-8)(x+1)$ . Since  $(3x)(1) + (-8)(x) = -5x \neq -10x$ , this doesn't work.

$(3x+2)(x-4)$ . Since  $(3x)(-4) + (2)(x) = -10x$ , this is the correct factorization!

Check your factorization by FOILing it out. You should get your original trinomial.

$3x^2 - 10x - 8$   
 $(3x^2 - 12x) + (2x - 8)$   
 $3x(x-4) + 2(x-4)$   
 $(x-4)(3x+2)$

$\left. \begin{array}{l} a \cdot c \\ 3 \cdot -8 = -24 \\ -12 \times 2 = -24 \\ -10 \\ b \end{array} \right\}$

$\left. \begin{array}{l} -24 \\ -4 \\ -12 \\ 2 \\ 3x \\ -10 \\ 3x \end{array} \right\}$

$(x-4)(3x+2)$

YOUR TURN: Factor each of the following trinomials.

a)  $2y^2 - y - 6$

b)  $8x^2 + 6x - 5$

$(8x^2 - 4x) + (10x - 5)$   
 $(4x)(2x-1) + 5(2x-1)$   
 $(2x-1)(4x+5)$

$\left. \begin{array}{l} -40 \\ 10 \\ -4 \\ 6 \end{array} \right\}$

$(4x+5) \leftarrow \frac{5}{4x} \leftarrow \frac{10}{8x} \leftarrow \frac{-4}{8x} \rightarrow \frac{-1}{2x} \rightarrow (2x-1)$   
 $(4x+5)(2x-1)$

c)  $6t^2 + t - 15$

d)  $2y^2 + 9y + 9$

*Special patterns to watch for:*

1.  $a^2 + 2ab + b^2 = (a + b)^2$

EXAMPLE:  $16 + 8x + x^2$  - Notice that  $16 = 4^2$ , so  $a = 4$  and  $x^2 = b^2$ , so  $b = x$ . In addition,  $8x = 2 \cdot 4 \cdot x = 2ab$ . This fits the pattern, so the factorization is  $(4 + x)^2$ .

2.  $a^2 - 2ab + b^2 = (a - b)^2$

EXAMPLE:  $25x^2 - 20x + 4$  - Notice that  $25x^2 = (5x)^2$ , so  $a = 5x$  and  $4 = 2^2$ , so  $b = 2$ . In addition,  $20x = 2 \cdot 5x \cdot 2 = 2ab$ . This fits the pattern, so the factorization is  $(5x - 2)^2$ .

3.  $a^2 - b^2 = (a + b)(a - b)$

EXAMPLE:  $9t^2 - 64$  - Notice that  $9t^2 = (3t)^2$ , so  $3t = a$ , and  $64 = 8^2$ , so  $8 = b$ . This fits the pattern, so the factorization is  $(3t + 8)(3t - 8)$ .

YOUR TURN: Factor each of the following.

a)  $x^2 - 49$

b)  $36y^2 - 12y + 1$

c)  $n^2 + 18n + 81$

d)  $25y^4 - 100$

*Summary:*

- Always factor out any common factors first.
- Factor any remaining trinomials or binomials, if possible, using the instructions given above. If the remaining trinomial or binomial cannot be factored, leave it.

Homework

Factoring Worksheet