

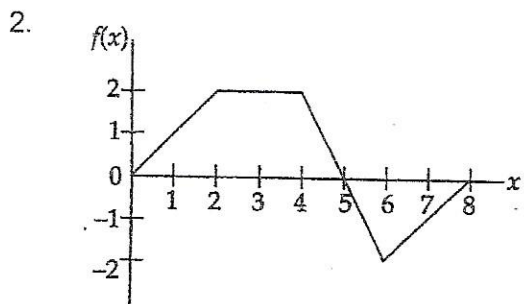
Name: _____ Date: _____

AP CALCULUS AB
Unit 6 Review
Definite Integrals

No calculator may be used on the following problems.

1. $\int_2^3 \frac{1}{x^3} dx =$

- (A) $-\frac{5}{72}$ (B) $-\frac{5}{36}$ (C) $\frac{5}{144}$ (D) $\frac{5}{72}$ (E) $\ln \frac{27}{8}$



The graph of a piecewise linear function f , for $0 \leq x \leq 8$, is shown above. What is the value of $\int_0^8 f(x) dx$?

- (A) 1 (B) 4 (C) 8 (D) 10 (E) 13

3. If $\int_a^b f(x) dx = 5$ and $\int_a^b g(x) dx = -1$, which of the following must be true?

- I. $f(x) > g(x)$ for $a \leq x \leq b$
II. $\int_a^b [f(x) + g(x)] dx = 4$
III. $\int_a^b [f(x)g(x)] dx = -5$

- (A) I only (B) II only (C) III only (D) II and III only (E) I, II, and III

4. If f is continuous for $a \leq x \leq b$, then at any point $x = c$, where $a < c < b$, which of the following must be true?

(A) $f(c) = \frac{f(b) - f(a)}{b - a}$

(B) $f(a) = f(b)$

(C) $f(c) = 0$

(D) $\int_a^b f(x) dx = f(c)$

(E) $\lim_{x \rightarrow c} f(x) = f(c)$

5. The average value of $\sec^2 x$ on the interval $\left[\frac{\pi}{6}, \frac{\pi}{4}\right]$ is

(A) $\frac{8}{\pi}$

(B) $\frac{12\sqrt{3} - 12}{\pi}$

(C) $\frac{12 - 4\sqrt{3}}{\pi}$

(D) $\frac{6\sqrt{2} - 6}{\pi}$

(E) $\frac{6 - 6\sqrt{2}}{\pi}$

6. $\int_{\frac{\pi}{2}}^x \cos t dt =$

(A) $-\sin x$

(B) $-\sin x - 1$

(C) $\sin x + 1$

(D) $\sin x - 1$

(E) $1 - \sin x$

A graphing calculator may be used for the following problems.

7. The expression $\frac{1}{30} \left(\sin \frac{1}{30} + \sin \frac{2}{30} + \sin \frac{3}{30} + \dots + \sin \frac{30}{30} \right)$ is a Riemann sum approximation for

- (A) $\int_0^1 \sin \frac{x}{30} dx$
(B) $\int_0^1 \sin x dx$
(C) $\frac{1}{30} \int_0^1 \sin \frac{x}{30} dx$
(D) $\frac{1}{30} \int_0^1 \sin x dx$
(E) $\frac{1}{30} \int_0^{30} \sin x dx$

8. $\frac{d}{dx} \int_0^{x^2} \sin^2 t dt =$

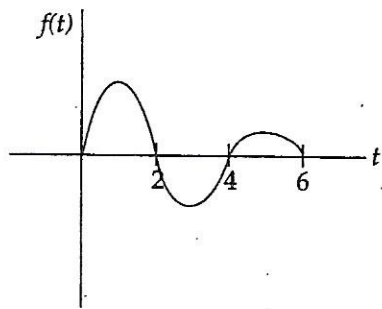
- (A) $x^2 \sin^2(x^2)$
(B) $2x \sin^2(x^2)$
(C) $\sin^2(x^2)$
(D) $x^2 \cos^2(x^2)$
(E) $2x \cos^2(x^2)$

9. A continuous function $h(t)$ is defined in the closed interval $[10, 16]$ with values given in the table below. Using the data, estimate $\int_{10}^{16} h(t) dt$ using a trapezoidal approximation with three subintervals of unequal length.

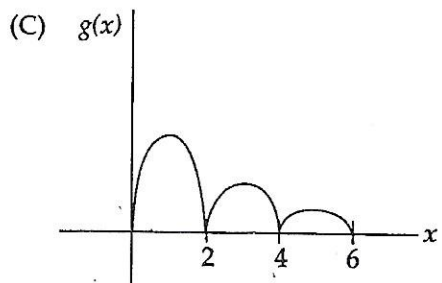
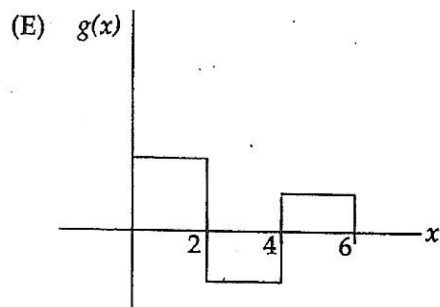
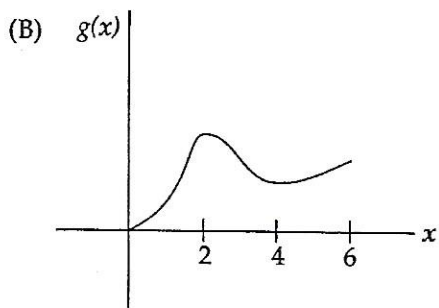
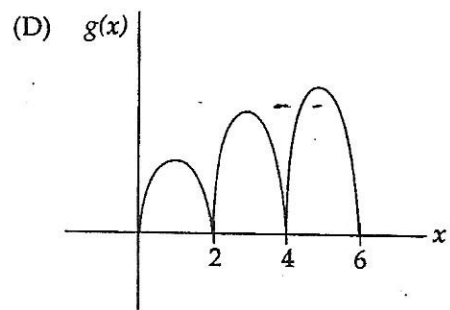
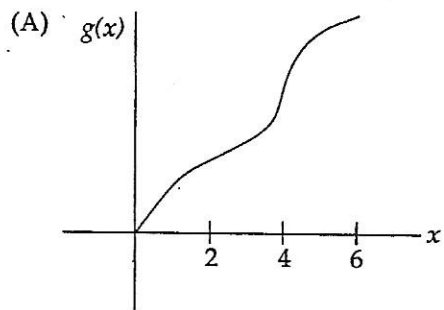
t	10	12	15	16
$h(t)$	10	20	50	80

- (A) $\frac{359}{3}$ (B) 130 (C) 200 (D) 270 (E) 718

10.



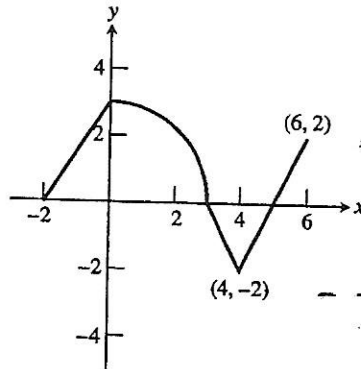
Let $g(x) = \int_0^x f(t) dt$, where $f(t)$ has the graph shown above. Which of the following could be the graph of g ?



FREE RESPONSE. No calculator may be used for Problem 11.

11. The graph of g shown in the figure consists of a quarter-circle and three line segments. Let h be the function defined by

$$h(x) = \int_0^x g(t) dt$$



(a) Evaluate $h(4)$.

(b) Find all values of x in the interval $[-2, 6]$ at which h has a relative minimum. Justify your answer.

(c) Find the value of $h'(2)$.

(d) Find the x -coordinate of each point of inflection of the graph of h on the interval $(-2, 6)$. Justify your answer.