

Questions on 7.5 HW?

SM3H - Module 7 - Student Edition.pdf - Adobe Acrobat Reader DC

File Edit View Window Help

Home Tools SM3H - Module 7 ... x

33 / 52 125%

Use the table to find the indicated function values.

x	f(x)	g(x)
-2	2	3
-1	1	-2
0	3	-24
1	-1	-1
2	0	-8
3	19	0

©2014 www.flickr.com/photos/scobleizer

1. $f(g(3)) =$ $g(3) = 0$
 $f(0) = 3$

2. $f(g(1)) =$ $g(1) = -1$
 $f(-1) = 1$

3. $g(f(-2)) =$ $f(-2) = 2$
 $g(2) = -8$

4. $g(f(-1)) =$ $f(-1) = 1$
 $g(1) = -1$

5. $g(f(0)) =$ $f(0) = 3$
 $g(3) = 0$

6. $g(g(-2)) =$ $g(-2) = 3$
 $g(3) = 0$

7. $f(f(0)) =$ $f(0) = 3$
 $f(3) = 19$

8. $g(f(1)) =$ $f(1) = -1$
 $g(-1) = -2$

9. Do the graphs ever intersect each other?
 How do you know?

SM3H - Module 7 - Student Edition.pdf - Adobe Acrobat Reader DC

File Edit View Window Help

Home Tools SM3H - Module 7 ... x

33 / 52 125%

9. Do the graphs ever intersect each other?
How do you know?

Use the graph to find the indicated values.

10. $f(g(-2)) = f(2) = 6$ 11. $f(g(-1))$

12. $f(g(1.5))$ 13. $f(f(0))$

Mathematics Vision Project | MVP
Licensed under the Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported license

8.50 x 11.00 in

SM3H - Module 7 - Student Edition.pdf - Adobe Acrobat Reader DC

File Edit View Window Help

Home Tools SM3H - Module 7 ... x

34 / 52 125%

Topic: Creating a composite function given its components

Let $f(x) = x^2$, $g(x) = 5x$, and $h(x) = \sqrt{x} + 2$.
Express each function as a composite of f , g , and/or h .

14. $F(x) = x^4$ 15. $G(x) = 5x^2$ 16. $P(x) = x + 2$

17. $R(x) = 5\sqrt{x} + 10$ 18. $Q(x) = 25x$ 19. $H(x) = 25x^2$

20. $D(x) = \sqrt{\sqrt{x} + 2} + 2$ 21. $B(x) = x + 4\sqrt{x} + 4$ 22. $K(x) = \sqrt{5x} + 2$

Go Topic: Finding the zeros of a polynomial

Handwritten notes in blue ink:

- $f(g(x)) =$
- $g(f(x)) =$
- $f(h(x)) =$
- $5(\sqrt{x} + 2)$ (with an arrow pointing to $h(x)$)
- $g(h(x))$
- $f(h(x)) = (\sqrt{x} + 2)^2$

8.50 x 11.00 in

SM3H - Module 7 - Student Edition.pdf - Adobe Acrobat Reader DC

File Edit View Window Help

Home Tools SM3H - Module 7 ... x

34 / 52 125%

Solve for all of the values of x . Identify any restrictions on x .

23. $x^2 + 6 = 5x$

24. $5x^3 = 45x$

25. $x^4 - 26x^2 + 25 = 0$

26. $1 + \frac{1}{x} = \frac{12}{x^2}$

27. $\frac{x}{6} - \frac{1}{2} - \frac{3}{x} = 0$

28. $\frac{1}{x^2} = 9$

$ax^2 + bx + c$
 $x^2 + 0x - 1$

$(x^2 - 1)(x^2 - 25) = 0$
 $(x - 1)(x + 1)(x - 5)(x + 5) = 0$
 $x = 1, -1, 5, -5$

Mathematics Vision Project | MVP
 Licensed under the Creative Commons Attribution-NonCommercial-ShareAlike 3.0 Unported license

8.50 x 11.00 in

7.6 Different Combinations

A Practice Understanding Task

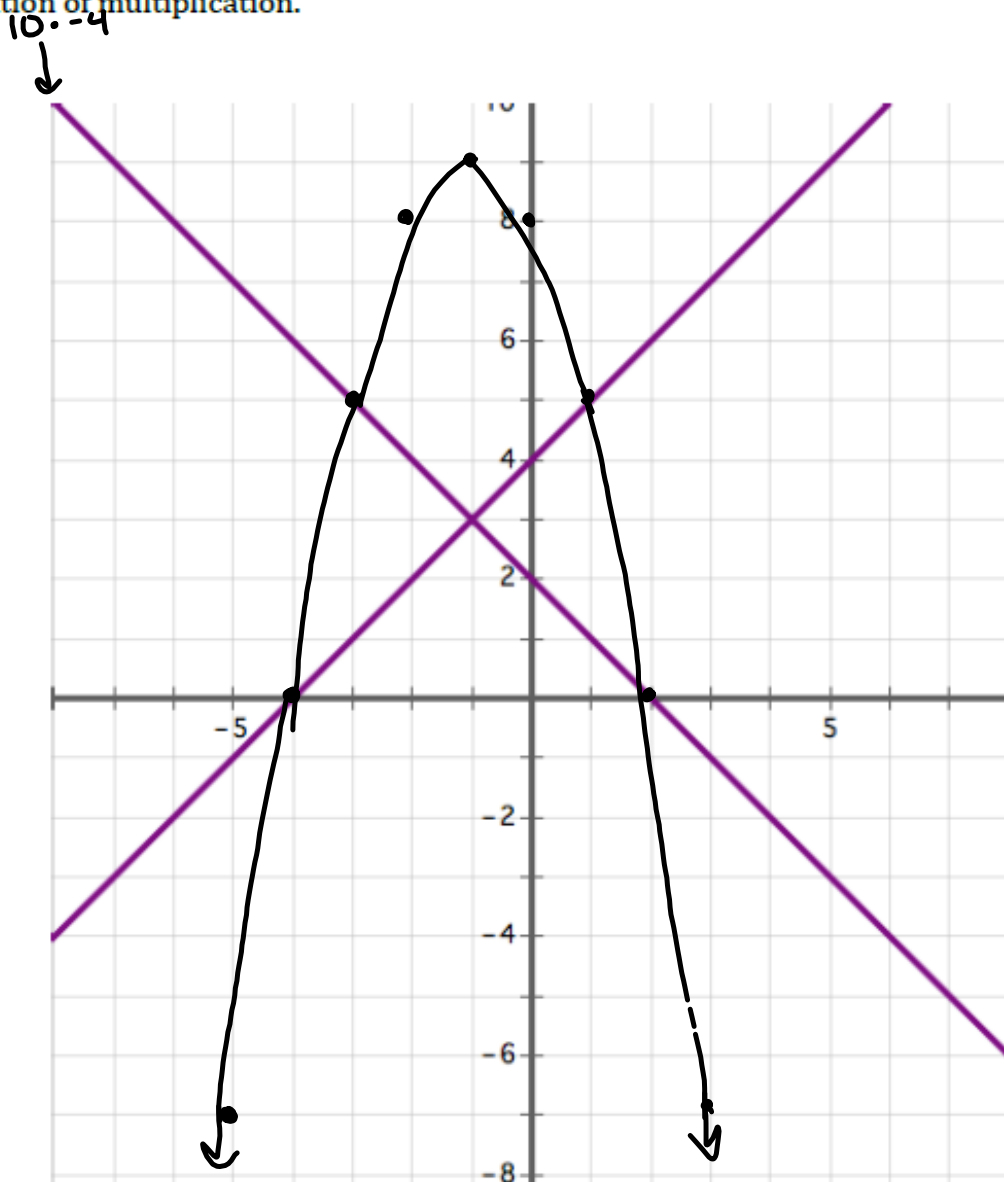
We have found the value of being able to combine different function types in various ways to model a variety of situations. In this task you will practice combining functions when they are described in different ways: graphically, numerically or algebraically.

1. Add the following two functions together graphically. That is, do not write the algebraic rules for each individual function, add them together, and then graph the result. See if you can produce the resulting graph by just working with the points on the two graphs and considering what happens when two functions are combined using the operation of addition.



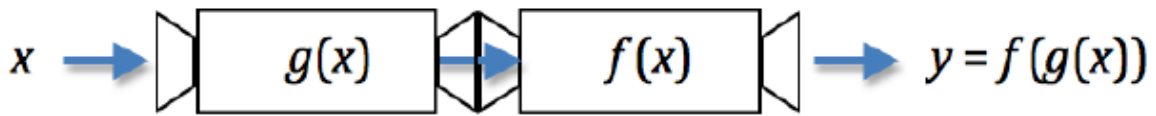
What points are most helpful in determining the shape of the resulting graph, and why?

2. **Multiply** the following two functions together graphically. That is, do not write the algebraic rules for each individual function, multiply them together, and then graph the result. See if you can produce the resulting graph by just working with the points on the two graphs and considering what happens when two functions are combined using the operation of multiplication.



What points are most helpful in determining the shape of the resulting graph, and why?

3. In a previous task we used the following diagram to illustrate function composition. Draw a similar type of diagram to illustrate what happens when two functions are combined by addition or multiplication. Your diagram should clearly show how the output values are obtained for specific input values.



4. Functions f and g are defined numerically in the following table. No other points exist for these functions other than the points given. Find the output values for each of the other combinations of functions indicated. Fill in as many points as are defined based on the give data. Use the same input values for all functions.

domain $x-2$	range $f(x)-4$	$g(x)$	$(f+g)(x)$	$f^{-1}(x)$	$g(f(x))$	$f(g(x))$
0	0	-3	-3	0	$g(0) = -3$	$f(-3) = -6$
1	2	-2	0	1	$g(2) = -1$	$f(-2) = -4$
→ 2	$f(2) = 4$	$g(2) = -1$	$f(2)+g(2) = 4+(-1) = 3$	2	$g(f(2)) = g(4) = 1$	$f(g(2)) = f(-1) = -2$
3	6	0	6	3	$g(6) = 3$	$f(0) = 0$
4	$f(4) = 8$	$g(4) = 1$	9	4	$g(8) = 5$	$f(1) = 2$
5	10	2	12	5	$g(10) = 7$	$f(2) = 4$
6	12	3	15	6	$g(12) = 9$	$f(3) = 6$
7	14	4	18	7	$g(14) = 11$	$f(4) = 8$
8	16	5	21	8	$g(16) = 13$	$f(5) = 10$

9
10
11
12
13
14
15
16

6
7
8
9
10
11
12
13

5. Remember the race between the tortoise and the hare? Well, their friends and families have come to cheer them on, and have positioned themselves at various places along the course. Because rabbits are quick and eager to know the outcome of the race, more of them have congregated towards the end of the course. Because turtles are slow and more anxious to cheer their champion off to a good start, more of them have congregated at the beginning of the race. In fact, the density (or amount of animals/meter) of turtles and rabbits along the course as a function of the distance from the starting line is given by the following functions.

The tortoise: $a(d) = 243 \cdot \left(\frac{1}{3}\right)^{\frac{1}{20}d}$ (a is in turtles per meter, d in meters)

The hare: $a(d) = 2^{\frac{1}{10}d}$ (a is in rabbits per meter, d in meters)

The distance from the starting line, as a function of the elapsed time since the start of the race, is given for the tortoise and the hare by the following functions.

The tortoise: $d(t) = 2^t$ (d in meters, t in seconds)

The hare: $d(t) = t^2$ (d in meters, t in seconds)

The tortoise and the hare are anxious to know how many of their friends and family they are passing at any instant in time along the race.

- Create functions for the tortoise and for the hare that will calculate the number of turtles or rabbits they will pass at any time, t , after the race begins. Include a reasonable domain for each function.
- If the race is 100 meters long, create a function that will tell how many spectators, rabbits and turtles, are watching at any distance away from the start of the race?
- Who is passing the most friends and families, the tortoise or the hare, 5 seconds after the race began?

Homework

Finish 7.6 "Ready, Set, Go"