Questions on Chapter 3/

Patterns Assessment Review?

We will be taking our Patterns

Assessment as soon as possible!

SIZE	tyles avadr.	sum of all
12345	1>2 3>3>1 4>1 10>5 15:	10 > 10 > 3 > 1 20 > 10 > 5 > 1 35 > 16
7	$\frac{1}{2}x^2 + \frac{1}{2}x$ $\frac{n(n+1)}{2}$	$\frac{n(n+1)(n+2)}{6}$

Patterns Assessment

Grab a book and tear out chapter 5 (pg. 313-422). We are skipping chapter 4, but feel free to tear it out for yourself if you need additional practice with quaadratic functions.

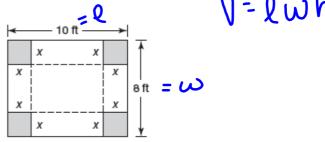


Planting the Seeds Exploring Cubic Functions

NOT IN YOUR BOOK

1. Cynthia is an engineer at a manufacturing plant. Her boss asks her to use rectangular metal sheets to build storage bins with the greatest possible volume. Each rectangular sheet is 8 feet by 10 feet.

Cynthia's sketch shows the squares to be removed from the corners of each sheet. The dashed lines indicate where the metal sheets will be folded before they are welded to form the prism-shaped storage bins without tops.



a. Complete the table.

0	8	Ū	0
	_		
	6	8	48
2	4	6	48
3	2	4	24
4	O	2	O
-	2 3 4	2 4 3 2 4 0	2 4 6 3 2 4 4 0 2

b. Write a function V(x) to represent the volume of a bin in terms of the side length, x, of the removed squares. Explain your reasoning.

$$V(x) = X(8-2x)(10-2x)$$

$$X(80 - 16x - 20x + 4x^{2})$$

$$80x - 16x^{2} - 20x^{2} + 4x^{3}$$

$$80x - 36x^{2} + 4x^{3}$$

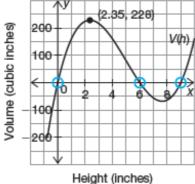
STILL NOT IN YOUR BOOK

V(x) = X (8-2x)(10-2x) $V(x) = 80x - 36x^2 + 4x^3$ c. Represent the function V(x) on a graphing calculator. Determine the domain and range of the

- c. Represent the function V(x) on a graphing calculator. Determine the domain and range of the function. Determine the domain and range of the function as they relate to the problem situation. Explain your reasoning.
 (44) 29 329-337
- d. Determine the maximum volume of a bin. What are the dimensions of a bin with the maximum volume?
- e. Determine any relative maximums or relative minimums of V(x). Then, determine the intervals over which the function is increasing and decreasing.
- f. Determine the x- and y-intercepts of the graph of V(x). What do they represent in this problem situation?
- g. Cynthia's boss asks her to make several bins with volumes of exactly 40 cubic feet. Determine the bin dimensions that will work.

PG.320 IN YOUR BOOK

The key characteristics of a function may be different within a given domain. The function V(h) = h(12 - 2h)(18 - 2h) has x-intercepts at x = 0, x = 6, and x = 9.



As the input values for height increase, the output values for volume approach infinity. Therefore, the function doesn't have a maximum; however, the point (2.35, 228) is a relative maximum within the domain interval of (0, 6). A relative maximum is the highest point in a particular section of a graph. Similarly, as the values for height decrease, the output values approach negative infinity. Therefore, a relative minimum occurs at (7.65, -68.16). A relative minimum is the lowest point in a particular section of a graph.

The function v(h) represents all of the possible volumes for a given height h. A horizontal line is a powerful tool for working backwards to determine the possible values for height when the volume is known.

PG.326 IN YOUR BOOK

The volume functions for the rectangular planter box and the cylindrical shaped planter are examples of *cubic functions*. A **cubic function** is a function that can be written in the standard form $f(x) = ax^3 + bx^2 + cx + d$ where $a \ne 0$. In other words, a cubic function is a polynomial function of degree 3.

The volume of the rectangular planter box was represented as V(h) = h(12 - 2h)(18 - 2h). You can multiply the three factors to express the function in standard cubic form.

$$V(h) = h(12 - 2h)(18 - 2h)$$

$$= h(216 - 60h + 4h^{2})$$

$$= 216h - 60h^{2} + 4h^{3}$$

$$V(h) = 4h^{3} - 60h^{2} + 216h$$

The volume of the cylindrical shaped planter was represented as $V(x) = (3.14x^2)(2x)$. You can multiply the two factors to express the function in standard cubic form.

$$V(x) = 6.28x^3$$

The Fundamental Theorem of Algebra tells you that a cubic function must have 3 zeros. Roots may be any number in the set of complex numbers, and can even appear multiple times. **Multiplicity** is how many times a particular number is a zero for a given polynomial function. For example in the polynomial function that represents the volume of the cylindrical shaped planter, $V(x) = (3.14x^2)(2x)$, the zero, x = 0, has multiplicity 3.

PG.329 IN YOUR BOOK

- 3. Determine each product. Show all your work and then use a graphing calculator to verify your product is correct.
 - a. (x + 2)(-3x + 2)(1 + 2x)



NOT IN YOUR BOOK

2. Write a cubic function with zeros of -4, 2, and 3. Write the function in the form $f(x) = ax^3 + bx^2 + cx + d$. Verify graphically that the function has the correct zeros.

- 3. Consider the given functions.
 - f(x) = x + 2
 - $g(x) = x^2 3.5x + 2.5$
 - $h(x) = f(x) \cdot g(x) = (x + 2)(x^2 3.5x + 2.5)$
 - **a.** Determine the zeros of f(x), g(x), and h(x).
 - **b.** How are the zeros of h(x) related to the zeros of f(x) and g(x). Explain why this is true.
 - **c.** Write a function m(x) that has the same zeros as h(x) plus an additional zero of 5. Verify your answer graphically.

Homework

Finish lesson 5.1