

If I don't have your Unit 4 homework, get out your outline so I can check your homework off and collect your outline.

Work on the problem below...

Happy Birthday  
Tilda!

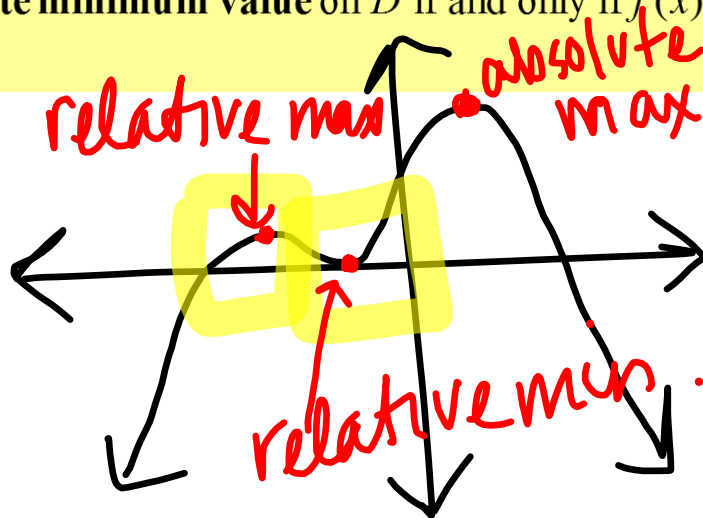
## 5.1 Extreme Values of Functions

### Absolute Extreme Values

Let  $f$  be a function with domain  $D$ . Then  $f(c)$  is the

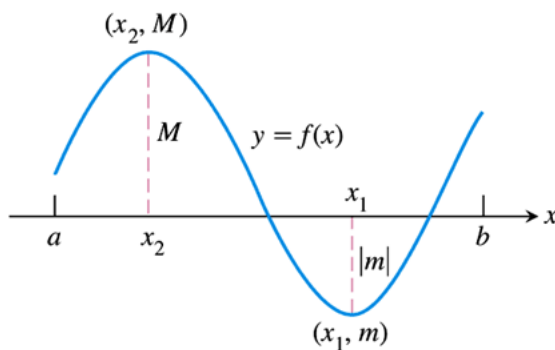
(a) **absolute maximum value** on  $D$  if and only if  $f(x) \leq f(c)$  for all  $x$  in  $D$ .

(b) **absolute minimum value** on  $D$  if and only if  $f(x) \geq f(c)$  for all  $x$  in  $D$ .

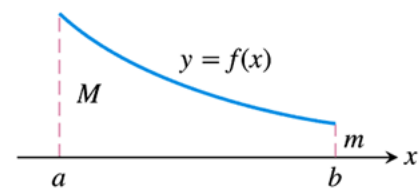


# The Extreme Value Theorem EVT

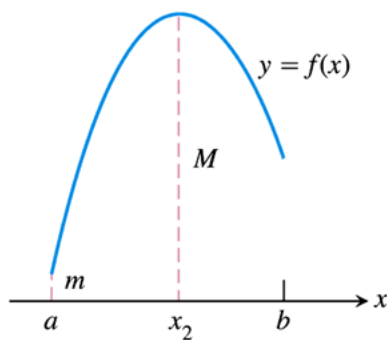
If  $f$  is continuous on a closed interval  $[a, b]$ , then  $f$  has both a maximum value and a minimum value on the interval.



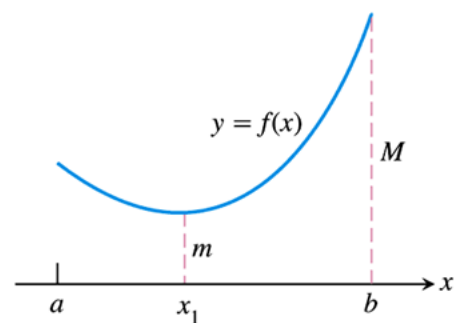
Maximum and minimum at interior points



Maximum and minimum at endpoints

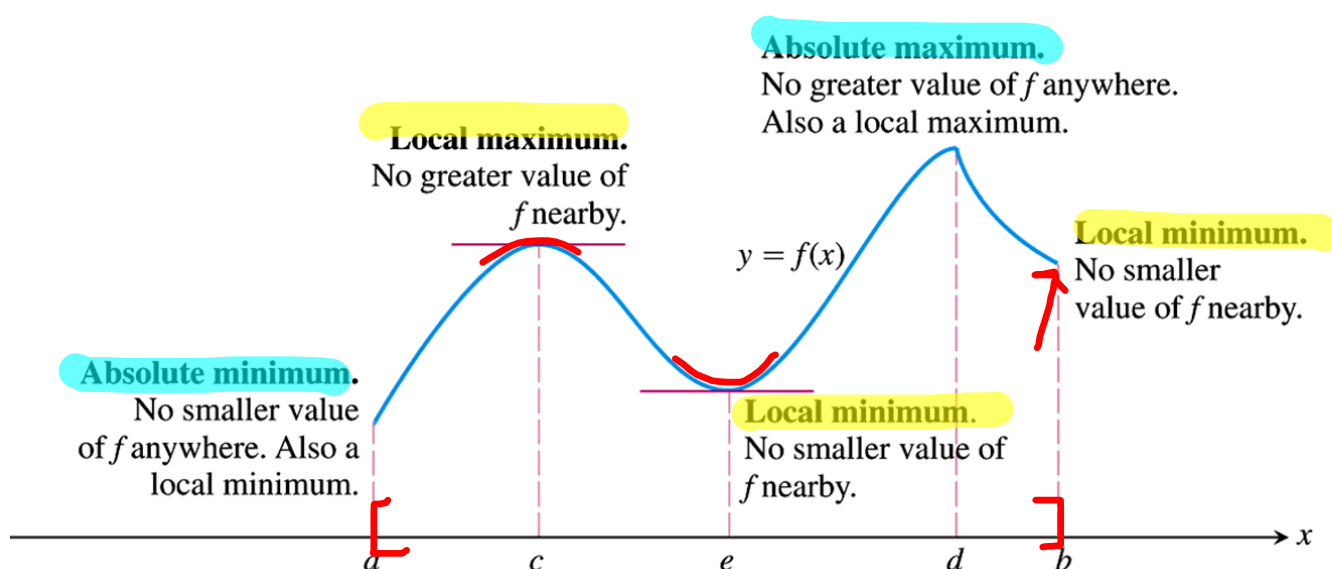


Maximum at interior point, minimum at endpoint



Minimum at interior point, maximum at endpoint

## Classifying Extreme Values



closed interval  $[a, b]$

## Local Extreme Values

Let  $c$  be an interior point of the domain of the function  $f$ . Then  $f(c)$  is a **(a) local maximum value** at  $c$  if and only if  $f(x) \leq f(c)$  for all  $x$  in some open interval containing  $c$ .

**(b) local minimum value** at  $c$  if and only if  $f(x) \geq f(c)$  for all  $x$  in some open interval containing  $c$ .

A function  $f$  has a local maximum or local minimum at an endpoint  $c$  if the appropriate inequality holds for all  $x$  in some half-open domain interval containing  $c$ .

horizontal tan lines @ local mins & local max's

If a function  $f$  has a local maximum value or a local minimum value at an interior point  $c$  of its domain, and if  $f'$  exists at  $c$ , then  $f'(c) = 0$ .

## Critical Points

A point in the interior of the domain of a function  $f$  at which  $f' = 0$  or  $f'$  does not exist is a **critical point** of  $f$ .

## Examples

1. Find all local and global extrema of  $f(x) = \frac{1}{3}x^3 - \frac{5}{2}x^2 - 14x + 7$ .

2. Find all absolute and relative extrema of  $g(x) = \begin{cases} 5 - 2x^2 & , x \leq 1 \\ x + 2 & , x > 1 \end{cases}$ .

3. Find all global and local extrema of  $h(x) = \frac{x}{1+x^2}$ .

## Examples

1. Find all local and global extrema of  $f(x) = \frac{1}{3}x^3 - \frac{5}{2}x^2 - 14x + 7$ .

$$f'(x) = x^2 - 5x - 14$$

$$0 = x^2 - 5x - 14$$

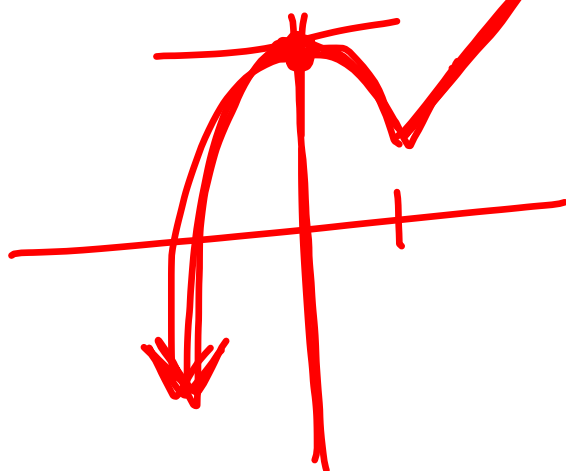
$$0 = (x - 7)(x + 2)$$

$$x = 7, -2$$

2. Find all absolute and relative extrema of  $g(x) = \begin{cases} 5 - 2x^2, & x \leq 1 \\ x + 2, & x > 1 \end{cases}$ .

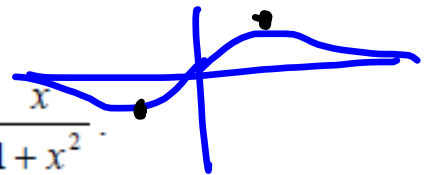
$$g'(x) = \begin{cases} -4x & \rightarrow 0 = -4x \\ 1 & \rightarrow \frac{-4}{-4} = \frac{-4}{-4} \end{cases}$$

$$0 = x$$





3. Find all global and local extrema of  $h(x) = \frac{x}{1+x^2}$ .



$$h'(x) = \frac{(1+x^2) \cdot 1 - x(2x)}{(1+x^2)^2}$$

$$h'(x) = \frac{1+x^2-2x^2}{(1+x^2)^2} = \frac{-x^2+1}{(1+x^2)^2}$$

$$\begin{aligned} 0 &= -x^2 + 1 \\ x^2 &= 1 \\ x &= \pm 1 \end{aligned}$$

Just set numerator equal to 0.

$$\frac{0}{w} = 0$$

## Homework

5.1 pg.198 #3-30 (X3), 35, 37, 40