

Quiz today, but first...questions  
on 3.6 HW?

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Topic: Factoring Special Products

sum/difference of cubes

$$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$$
$$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$$

1.  $4x^2 - 25$

2.  $9x^2 - 16y^2$

3.  $a^2x^2 - b^2$

4.  $64x^3 - 125$

$a=4x$

$b=5$

5.  $27x^3 + 8$

$= (4x-5)((4x)^2 + (4x \cdot 5) + 5^2)$

$= (4x-5)(16x^2 + 20x + 25)$

6.  $1000x^3 - y^3$

**Set**

Topic: Find all zeros of each polynomial then sketch the graph. Use technology if needed.

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3.  $a^2x^2 - b^2$

4.  $64x^3 - 125$

5.  $27x^3 + 8$   $\therefore (3x+2)(9x^2 - 6x + 4)$   
 $a = 3x$

6.  $1000x^3 - y^3$   $(3x+2)((3x)^2 - (3x)(2) + (2)^2)$

sum/difference of cubes

$a^3 + b^3 = (a+b)(a^2 - ab + b^2)$

$a^3 - b^3 = (a-b)(a^2 + ab + b^2)$

Set

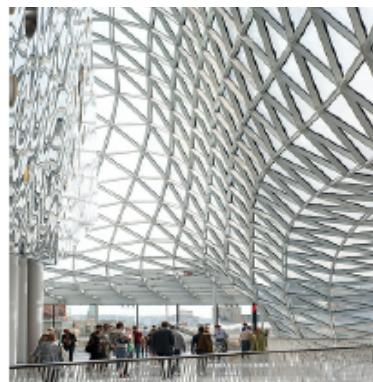
Topic: Find all zeros of each polynomial, then sketch the graph. Use technology.

7.  $f(x) = x^2 - 25$

8.  $g(x) = 4x^2 - 9$

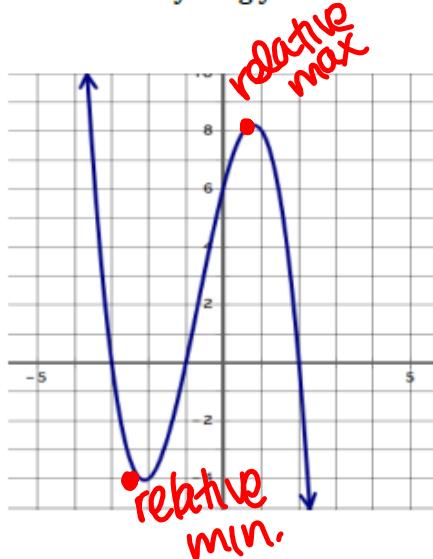
## 3.7 Graphing all Poly's

### A Solidify Understanding Task



Part I: Connecting the number system to polynomials.

1. Write everything you know about the following polynomial:



X-Intercepts:

$$x = -1, 2, 3$$

Points:  $(-1, 0), (2, 0), (3, 0)$

<http://www.flickr.com/photos/cu2nite/34778886>

(3rd degree)

y-intercept

$$y = 6 \quad (0, 6)$$

As  $x \rightarrow -\infty, f(x) \rightarrow \infty$  } negative L.Coeff.

As  $x \rightarrow \infty, f(x) \rightarrow -\infty$  }

2. In case this was not part of what you wrote in question 1, use function notation to highlight values of importance for this function. (For example:  $f(0) = 6$ )

$$f(-1) = 0$$

$$f(3) = 0$$

$$f(2) = 0$$

$$f(0) = 6$$

3. The graph above gives us quite a bit of information to assist in writing the equation. What if instead you have a polynomial function written out in standard form and are given one factor, how could you determine the graph of the function?

$$0 = -(x+1)(x+3)(x-2)$$

$$0 = (x^2 + 4x + 3)(x - 2)$$

$$0 = (x^3 + 4x^2 + 3x - 2x^2 - 8x - 6) = (x^3 + 2x^2 + 5x + 6)$$

For each, one factor of a cubic function is given. Do your best to find the remaining factors and then use this information to determine all roots of the function and sketch a graph.

4. Function:  $f(x) = x^3 + 3x^2 - 4x - 12$       Factor:  $(x + 3)$       Roots of function:

5. Function:  $f(x) = x^3 + 6x^2 + 11x + 6$       Factor:  $(x + 1)$       Roots of function:

6. Function:  $f(x) = x^3 + 3x^2 - 12x - 12$  Factor:  $(x - 3)$

Roots of function:

7. Function:  $f(x) = x^3 - x^2 + 4x - 4$  Factor:  $(x - 2i)$

*3 roots*  

$$(x - 2i)(x + 2i)(\quad)$$

Roots of function:  
 $x = 2i, -2i,$

8. Function:  $f(x) = x^3 - 3x^2 - 3x - 9$  Factor:  $(x - 3)$

Roots of function:

9. Find all linear factors and graph:  $f(x) = x^4 - 16$

Roots of function:

Part II: Given the roots, find the factors and write the polynomial equation in standard form.

10. Roots: 3, -4, and 0

11. Roots: 5,  $2i$ ,  $-2i$

12. Roots:  $\sqrt{3}$ ,  $-\sqrt{3}$ , -2

13. Find the factored form of the cubic function with roots 2,  $3i$  and \_\_

14. Conclusion: What have you learned about polynomial functions as a result of this task?

## Homework

3.7 "Ready, Set, Go"