

Questions on 3.5 HW {pg.135-137 #3-30 (X3)}?

$$(15) \quad s = 24t - 4.9t^2$$

$$s = t(24 - 4.9t)$$

$$0 = t(24 - 4.9t)$$

$$t = 0, \frac{24}{4.9} \approx 4.9$$

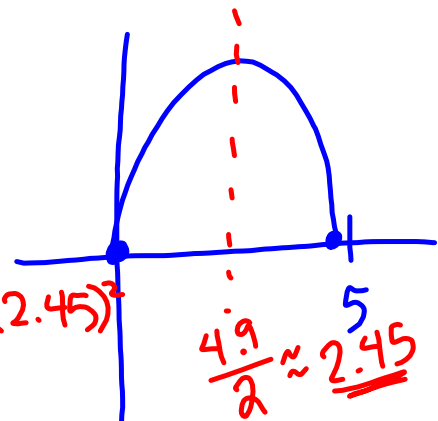
$$24 - 4.9t = 0$$

$$\frac{24}{4.9} = \frac{4.9t}{4.9}$$

$$4.9 \approx t$$

$$s(2.45) = 24(2.45) - 4.9(2.45)^2$$

$$s(2.45) = 29.388 \text{ m}$$



$$(24) \quad v = 2t^3 - 9t^2 + 12t - 5 \text{ m/sec}$$

$$a(t) = v' = 6t^2 - 18t + 12$$

$$0 = 6t^2 - 18t + 12$$

$$0 = 6(t^2 - 3t + 2)$$

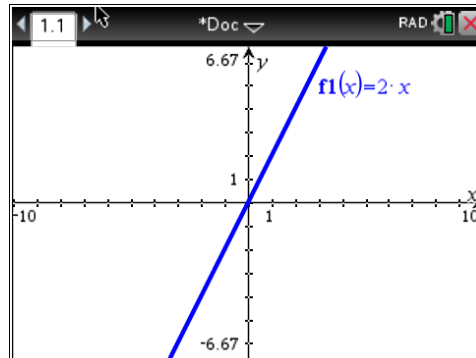
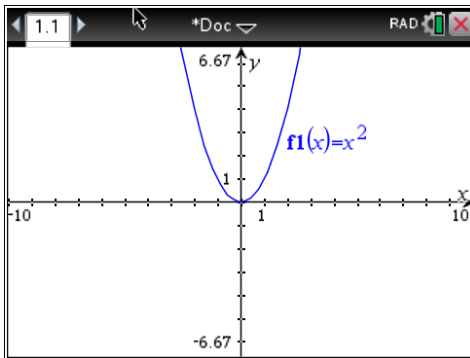
$$0 = 6(t - 2)(t - 1)$$

$$t = 2, 1 \text{ sec.}$$

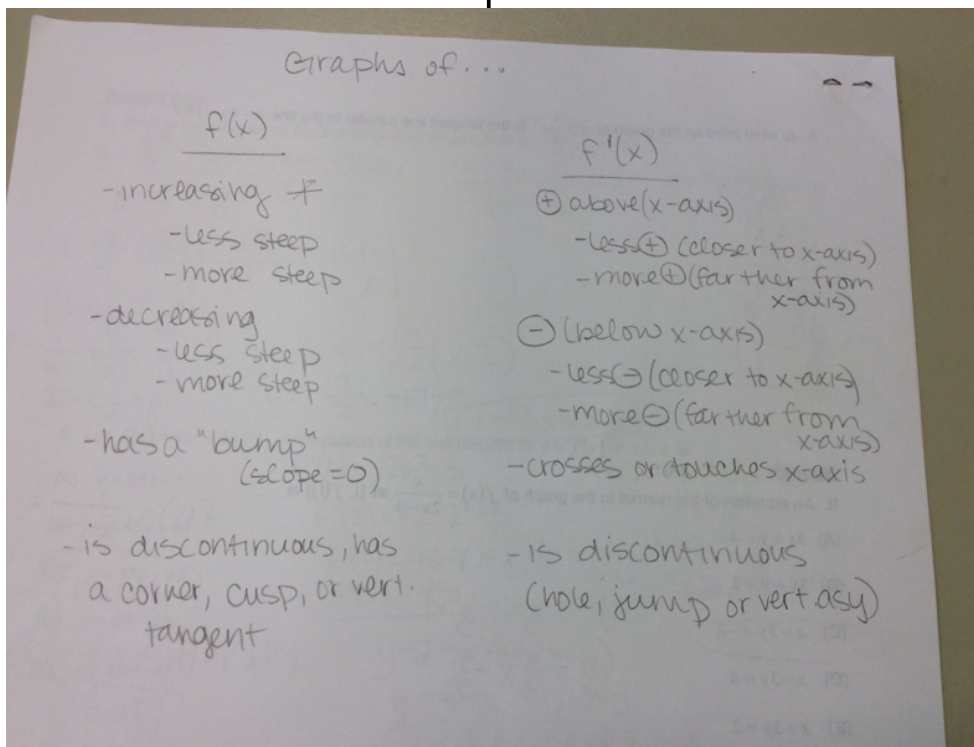
$$v(1) = 0 \text{ m/s}$$

$$v(2) = -1 \rightarrow 1 \text{ m/s}$$

Here's a  $f(x)$ .....and its  $f'(x)$



Comparing  $f(x)$  and  $f'(x)$ ...



**\*Graph Match Activity\***

Answers

- |   |    |   |    |
|---|----|---|----|
| A | 6  | G | 12 |
| B | 7  | H | 2  |
| C | 3  | I | 1  |
| D | 11 | J | 9  |
| E | 4  | K | 5  |
| F | 8  | L | 10 |

## 3.6 More Position, Velocity, Acceleration

<b><u>Important Terms</u></b>	
<b><u>Position Function</u></b>	gives the location of an object at time $t$ , usually $s(t)$ , $x(t)$ , or $y(t)$
<b><u>Velocity Function</u></b>	the rate of change (derivative) of position, usually $v(t)$ Velocity is positive for upward or rightward motion and negative for downward or leftward motion.
<b><u>Acceleration Function</u></b>	the rate of change (derivative) of velocity, usually $a(t)$
<b><u>Initial Position</u></b>	starting position (at $t = 0$ ), $s_0$
<b><u>Initial Velocity</u></b>	starting velocity (at $t = 0$ ), $v_0$
<b><u>Speed</u></b>	the absolute value of velocity
<b><u>Displacement</u></b>	the net change in position, (final pos. - original pos.)
<b><u>Total Distance</u></b>	total distance traveled by the object in the time interval (takes into account all direction changes)

Example 1. If  $s(t) = t^3 + t$ , find  $v(t)$  and  $a(t)$ .

$$s'(t) = v(t) = 3t^2 + 1$$

$$s''(t) = v'(t) = a(t) = 6t$$

Examples: Use the position function  $s(t) = 16t^3 - 36t^2 + 24$  of an object moving on a horizontal line for Examples 2-11. Distance units are measured in feet and time units are measured in seconds.

2. What is the initial position of the object?

$$s(0) = 24$$

3. What is the velocity of the object at  $t = 1$  second?

$$v(t) = 48t^2 - 72t$$

$$v(1) = 48 - 72 = -24 \text{ ft/sec}$$

4. What is the speed of the object at  $t = 1$  second?

$$\text{Speed} = 24 \text{ ft/sec}$$

5. What is the acceleration of the object at  $t = 1$  second?

$$a(t) = 96t - 72$$

$$a(1) = 96 - 72 = 24 \text{ ft/sec}^2$$

6. When is the object at rest?

$$\text{When } v(t) = 0$$

$$0 = 48t^2 - 72t$$

$$0 = 24t(2t - 3)$$

$$t = 0, \frac{3}{2} \text{ sec.}$$

7. When is the object moving right?

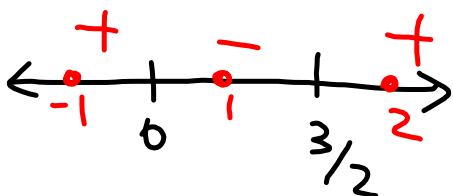
$$\text{When } v(t) > 0$$

$$t < 0 \text{ and } t > \frac{3}{2}$$

8. When is the object moving left?

$$\text{When } v(t) < 0$$

$$0 < t < \frac{3}{2}$$



9. When is the velocity of the object equal to  $54 \text{ ft/sec}$ ?

$$54 = 48t^2 - 72t$$

$$48t^2 - 72t - 54 = 0$$

doesn't factor nicely...

$$t = 0.549, 2.05$$

10. What is the displacement of the object between  $t = 0$  and  $t = 2$  seconds?

$$s(2) - s(0) =$$

$$8 - 24 =$$

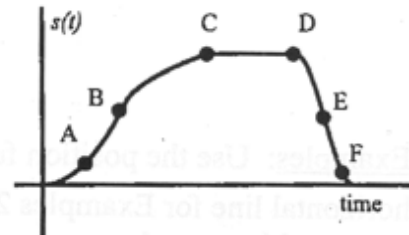
$$8 + 24 = \underline{32}$$

11. What is the total distance traveled by the object between  $t = 0$  and  $t = 2$  seconds?



The graph shows the position function of a radio controlled model car. Answer these questions and explain.

12. Was the car going faster at A or at B?
13. When was the car stopped?
14. At which point was the car's velocity the greatest?
15. At which point was the car's speed the greatest?



### Vertical Motion Examples:

Suppose  $s(t) = -16t^2 + 48t + 160$  gives the position (in feet) above the ground for a ball thrown into the air from the top of a high cliff (where time is measured in seconds).

16. Find the initial velocity.
17. At what time does the ball hit the ground?

# Homework

## 3.6 Worksheet